EQUILIBRIA IN MICELLAR SYSTEMS. PHOTOMETRIC DETERMINATION OF VANADIUM WITH 6-HYDROXY-5-DIBENZO(*a*,*j*)PHENOXAZONE--8,11-DISULPHONIC ACID ACTIVATED BY CETYLTRIMETHYLAMMONIUM BROMIDE

J.LASOVSKÝ^a and E.RUŽIČKA^b

^a Department of Inorganic and Physical Chemistry, and ^b Department of Analytical and Organic Chemistry, Palacký University, 771 46 Olomouc

Received May 28th, 1976

Dedicated to Professor S. Stankovianský on the occasion of his 70th birthday.

The reaction of cetyltrimethylammonium bromide (CTA⁺) with 6-hydroxy-5-dibenzo(*a,j*)phenoxazone-8,11-disulphonic acid (HL)* (I) was studied. At surfactant concentrations below the cmc, products with L: CTA⁺ = 1: 1 and 1: 2 are formed, the latter being stable in solution in the presence of a small excess of surfactant. The changes in the dye pK_a value can be explained on the basis of the common formalism of coordination reactions. Ternary complex VL_2S_4 is formed in the presence of vanadate in a weakly acid medium. The equilibrium constants for the ternary complex were determined, its existence region found and a photometric determination of vanadium proposed.

Surface-active substances have recently been employed for more sensitive photometric determinations of many ions. The increase in the molar absorption coefficients is explained by the formation of micellar system¹; sometimes the composition of the ion/dye/surfactant ternary complexes was found^{1.5}. Equilibria in micellar systems are also important for the explanation of the mechanism of micellar catalysis of organic reactions^{2-4,6}. Even here the changes in the rate constant values are usually connected with formation of micellar species^{2,3}, although the effect of the surfactant can sometimes be observed at concentrations lower than cmc (ref.^{4,6}). The phenomenon is explained by induced formation of micelles, protomicellar species or ion-associates⁴.

The present work was carried out in order to study the reaction between CTA^+ and the anionic dye (l) and to utilize the dye sensitized in this way for the determination of vanadium.

^{*} Ionic charges have been omitted for the sake of simplicity; pK_a corresponds only to ionization of the phenolic group.

EXPERIMENTAL

Chemicals and Instruments

A stock solution of the dye was prepared by dissolving the sodium salt in water at a concentration of 4 . 10^{-4} M. The dye purity was checked using elemental analysis and paper chromatography⁷. A cetyltrimethylammonium bromide solution was prepared in concentrations of 10^{-3} M and 4 . 10^{-2} M standard solution of sodium tetraphenylboron according to the Crosse and Uno method^{8,9}. A standard solution of vanadium was prepared by dissolving solid NH₄VO₃ in an equimolar amount of NaOH. The pH was maintained using formate, acetate and phosphate buffers and HCI solutions of various concentrations. If not stated otherwise, the ionic strength, *I*, was adjusted to a value of 0.1 using 1M-KCI. The absorbance was measured on Specord UV VIS (Zeiss, Jena) and Unicam SP 1800 (Cambridge, England) instruments in 1 and 5 cm cuvettes. The pH was measured on Beckman model G and PHM 62 (Radiometer, Copenhagen) instruments (\pm 0.02 pH).

Evaluation of the Experimental Data

The composition of the binary and ternary complexes was determined using the spectrophotometric titration¹⁰, continuous variation¹¹ and tangent ratio¹² methods. The stability constants were calculated numerically from the concentration curves (*I*) (*Ia*) and the absorption-pH curves (2) (2*a*),

$$A = f(c_{\rm S})_{\rm c_{L},pH,I}, \qquad (1)$$

$$A = f(c_{\rm V})_{c_{\rm L}, c_{\rm S}, pH, 1}; \quad c_{\rm S} > c_{\rm L}; \quad c_{\rm V},$$
(1a)

$$A = f(pH)_{c_L, c_S, 1}, \qquad (2)$$

$$A = f(pH)_{c_{L}, c_{V}, c_{S}, 1}; \quad c_{S} > c_{L}; \quad c_{V},$$
(2a)

where c_L , c_V and c_S are the overall analytical concentrations of the dye, vanadate and the surfactant, respectively. The dye ionization constants were measured spectrophotometrically in the usual manner. Only in the presence of the surfactant was the molar absorption coefficient of the ionized form obtained using transformation (3) (ref.¹³) for a pH region where no perceptible ionization of the dye occurs in pure solutions.

$$A/c_{\rm L} = \varepsilon_{\rm L} - [{\rm H}] A/K_{\rm a}c_{\rm L} .$$
⁽³⁾

RESULTS AND DISCUSSION

The first long-wave absorption bands of the two acid-base forms of the dye shift to longer wavelengths in the presence of surfactants. The changes in the molar absorption coefficients are insignificant (Table I). In acidic media (pH < 4.00), where only form HL is present (pK_a 7.37 \pm 0.04 in pure solutions or 6.09 \pm 0.02 at a surfactant concentration of c_s 2.98 \cdot 10⁻⁴M), the molar ratio curves indicate the formation of 1 : 1 products. The shape of the absorption curves (1) (c_L 8 \cdot 10⁻⁵M, pH 4.11) is not simple and indicates gradual formation

Equilibria in Micellar Systems

of micellar systems. In alkaline media (pH ≥ 10.4), absorption curves (1) in a concentration range of $c_{\rm S} \le 6 \cdot 10^{-5}$ M, $c_{\rm L} \ 1.6 \cdot 10^{-5}$ M pass through an isosbestic point, $\lambda_{\rm iso} 632$ nm. It was found by the spectrophotometric titration method ($c_{\rm L} \ 1.2 \cdot 10^{-4}$ M, pH 11.48; $c_{\rm L} \ 8 \cdot 10^{-5}$ M, pH 12.30; $c_{\rm L} \ 1.6 \cdot 10^{-5}$ M, pH 10.65) that complex LS₂ is formed (A)

$$L + 2S \rightleftharpoons LS_2$$
 (A)

Product LS₂ is stable in solution in the presence of a small CTA⁺ excess ($c_s \ge 3c_L$) and exists up to the surfactant cmc. The cmc for CTA⁺, obtained by extrapolation of conductometric measurements is $4 \cdot 10^{-4}$ M at $I \ 0.5$ (ref.⁴).

These equilibria are probably not connected with the formation of micellar species. The surfactant concentration is orders of magnitude smaller than the cmc and all the spectrophotometric titration curves obtained for various dye concentrations $(c_{\rm L} \ 1.6 \ .10^{-5} - 1.2 \ .10^{-4} {\rm M})$ indicate the presence of product LS₂. On plotting the absorbance dependence on the surfactant concentration at $\lambda_{\rm iso}$ of equilibrium (A), a further change in the absorbance appears at concentrations close to the cmc, $(2-4) \ .10^{-4} {\rm M}$. The same conclusions follow from absorption curves (1) for eosine, which is often employed for the determination of the cmc of cationoid surfactants¹⁴.

<i>c</i> _S (M)	λ _{max}	$\varepsilon_{\rm max}$. 10 ⁻³	
	form HL		
0	506	9.35	
2.10^{-4}	522	8.38	
4.10^{-4}	524	9.32	
0	513 ^a	10·82 ^a	
	L		
0	603	6.66	
0	620 ^a	6·75 ^a	
	LS ₂		
2.10-4	645	5.83	

TABLE I Absorption Maximum Wavelengths and the Molar Absorption Coefficients for Dye (1)

^a 50% (v/v) acetone.

Collection Czechoslov. Chem. Commun. [Vol. 42] [1977]

The yellow-green fluorescence of the pure dye disappears in the presence of small CTA⁺ concentrations ($c_{\rm S} < 10^{-4}$ M). The absorption maximum shifts to longer wavelengths and the spectrophotometric titration curves indicate the formation of products LS and LS₂ ($c_{\rm L} 1.28 \cdot 10^{-5}$ M, pH 5·63). At surfactant concentrations close to the cmc (2-4.10⁻⁴M), the formation of micellar systems is accompanied by a minute shift of the maximum of the first long-wave absorption band to shorter wavelengths and by reappearance of yellow-green fluorescence. In the presence of acetone the absorption maxima of the first long-wave bands of dye (1) are minutely shifted to longer wavelengths with a small increase in the absorption coefficients (Table I). The absorption maximum wavelengths do not change within a dye concentration range of $3\cdot 2 \cdot 10^{-4} - 1\cdot 6 \cdot 10^{-5}$ M. The shifts discussed are not caused by a change in the degree of association, but by simultaneous ionic and hydrophobic interactions leading to the formation of defined molecular complexes.



The presence of surfactant is manifested in the vicinity of the dye pK_a by a shift in the ionization equilibrium and by a large colour change. Equilibrium (B) can be formulated, characterized by equilibrium constant (4).

$$HL' + nS \rightleftharpoons LS_2 + H$$
 (B)

$$\beta_2' = [LS_2][H][HL']^{-1}[S]^{-n}$$

$$\tag{4}$$

[HL'] is the conditional concentration of the non-ionized dye form, including the possible product of the surfactant reaction localized on some of the sulpho groups. Only the LS₂ form absorbs around 700 nm and the equilibrium constant can be written as

$$\beta'_{2} = A(A_{0} - A)^{-1} [H][S]^{-n}$$
(5)

where $A_0 = \varepsilon l c_L$, or

$$\log A/A_0 - A = \log \beta'_2 + pH + n \log [S].$$
(5a)

It was found by the analysis of the concentration curves ($c_L 8.10^{-5}$ M, pH 5·18; 5·55; 5·59) and the pH-curves ($c_L 8.10^{-5}$ M, $c_S 2.98.10^{-4}$ M) that n = 1 and proposed

equilibrium (B) is correct, provided that HL' is identical with the HLS form. The latter can be found in the pH region where the dye is not ionized either in pure solutions or in the presence of surfactant. The stability constants were calculated numerically from the concentration and absorption pH curves ($c_L \ 8 \ 10^{-5} \text{M}$, pH 5·18; 5·55; 5·59 or $c_L \ 8 \ 10^{-5} \text{M}$, $c_S \ 2\cdot98 \ 10^{-4} \text{M}$) (Table II). In all cases excess surfactant was used to prevent associate formation. All measurements were carried out in 5 cm cuvettes in order not to exceed the surfactant cmc. The pK'a for the dye in the presence of the surfactant can be calculated from absorption pH curve (2) ($c_L \ 8 \ 10^{-5} \text{M}$, $c_S \ 2\cdot98 \ 10^{-4} \text{M}$). The ionization constant was calculated using the common procedure; only the absorption coefficient of form LS₂ was read from linear transformation (3). For $c_S \ 2\cdot98 \ 10^{-4} \text{M}$, pK'a is $6\cdot09 \pm 0\cdot02$. The presence of the surfactant in a concentration form the cmc causes an increase in the dye acidity by more than one order of magnitude.

Vanadate alone does not undergo a more important reaction with the dye studied and only a minute change in the colouration can be observed in equimolar mixtures. In the presence of CTA^+ , blue-green solutions of the ternary complex are formed in approximately equimolar mixtures of the dye and vanadate at pH 2·5-6·5. The colouration develops almost instantaneously and does not change for more than 24 hours. Vanadate oxidizes the dye irreversibly in acidic media (pH 2). The dye is more resistant toward this effect in the presence of CTA^+ and the oxidation is not observed in the studied pH interval. The vanadate reaction can analogously be made more pronounced with other dyes (pyrocatechol violet, alizarine sulphonate, *etc.*).

The absorption curves of solutions with constant concentrations of the dye and the surfactant and with a variable concentration of vanadate, obtained at pH 3.96, 4.08, 4.65 and 5.30, pass through an isosbestic point λ_{iso} 556 nm. The absorption curves

 $-\log \beta'_2(B)$	I	Equation	pK'a	I
 2.34	0.1	$(2)^{a}$	6.09 ± 0.02^{e}	0.1
2.36	0.1	$(1)^b$	_	
2.35	0.1	$(I)^{c}$	_	_
2.10	0.036	$(1)^d$	-	-

TABLE II						
Equilibrium	Constants	of the	CTA ⁺	/Dye	Binary	Comple:

^a $c_{\rm L}$ 8.10⁻⁵m, $c_{\rm S}$ 2.98.10⁻⁴m, average of 13 values converted to the logarithmic scale. ^b $c_{\rm L}$ 8.10⁻⁵m, pH 5.18, average of 5 values converted to the logarithmic scale. ^c $c_{\rm L}$ 8.10⁻⁵m, pH 5.55, average of 5 values converted to the logarithmic scale. ^d $c_{\rm L}$ 8.10⁻⁵m, pH 5.60, average of 6 values converted to the logarithmic scale. ^d $c_{\rm L}$ 8.10⁻⁵m, pH 5.60, average of 6 values converted to the logarithmic scale. ^d $c_{\rm L}$ 8.10⁻⁵m, pH 5.60, average of 6 values converted to the logarithmic scale. ^d $c_{\rm L}$ 8.10⁻⁵m, $c_{\rm S}$ 2.98.10⁻⁴m.

of equimolar solutions of vanadate and the dye containing excess surfactant pass through the same isosbestic point in a pH range of $2-3\cdot5$. The composition of the V/dye/ surfactant ternary complex was determined by spectrophotometric titration $(c_L 2\cdot56 . 10^{-5}\text{M}, c_S 4 . 10^{-4}\text{M}, \text{pH } 4\cdot08, 4\cdot63, 5\cdot21; \text{ or } c_L 8 . 10^{-5}\text{M}, c_S 4 . 10^{-4}\text{M}, \text{pH } 5\cdot30)$ $(c_L 8 . 10^{-5}\text{M}, c_V 2 . 10^{-4}\text{M}, \text{pH } 5\cdot35; \text{ or } c_L 12 . 10^{-4}\text{M}, c_V 2 \cdot 5 . 10^{-4}\text{M}, \text{pH } 6\cdot45)$, by the Job method $(c_0 8 . 10^{-5}\text{M}, \text{pH } 4\cdot08)$ and by the tangent ratio method, varying the vanadate concentration at excess dye and varying surfactants concentration with excess dye and vanadate. It was found that at complex ratios of V : : L 1 : 2, L : S 1 : 2 and V : $S 1 : 4 (\text{VL}_2\text{S}_4)$ is formed (C).

$$V + 2 HL + 4 S \rightleftharpoons VL_2S_4 + 2 H$$
 (C)

$$*\beta_{2,4} = [H]^{2} [VL_{2}S_{4}] [V]^{-1} [HL]^{-2} [S]^{-4}.$$
(6)

If only the complex absorbs at selected wavelengths (λ 670 nm) and dye ionization does not occur in the presence of the surfactant within the studied pH interval (pH \leq 3), then the association constant for equilibrium (C) is given by Eq. (6), or, for equimolar solutions of the dye and vanadate, by Eq. (7).

$$*\beta_{2,4} = [H]^2 A (2A_0 - A)^{-1} (1 - A/A_0)^{-2} (p - 2A/A_0)^{-4} c^{-6}, \qquad (7)$$

where A_0 is the horizontal branch of the pH-curve $(A = \varepsilon_1 c/2)$, c is the dye (vanadate) concentration and p is the surfactant excess $(p = c_s/c)$. With a sufficient surfactant excess, equilibrium constants (8) (8a) can be formulated.

$$*\beta_2 = [H]^2 A(2A_0 - A)^{-1} (1 - A/A_0)^{-2} c^{-2}, \qquad (8)$$

$$\log A(2A_0 - A)^{-1} (1 - A/A_0)^{-2} = \log *\beta_2 + 2 \,\mathrm{pH} + 2 \log c \,. \tag{8a}$$

Logarithmic transformation (8a) $(c_{\rm L} = c_{\rm V} \ 1.6 \ .10^{-5} \text{M}, \ c_{\rm S} \ 4 \ .10^{-4} \text{M})$ was linear over the whole steep part of the pH curve (pH 2-3), with a slope corresponding to two dissociated protons. Equilibrium constants $*\beta_{2,4}$ were calculated numerically from relationship (7) $(c_{\rm L} = c_{\rm V} \ 1.6 \ .10^{-5} \text{M}, \ c_{\rm S} \ 4 \ .10^{-4} \text{M})$ (Table III).

Conditional stability constants (9) were calculated from the absorbance differences at the equivalence point between the concentration curves, (1a), for the quantitative and the actual reaction ($c_L 2.56 \cdot 10^{-5}$ M, $c_S 6.4 \cdot 10^{-4}$ M, pH 4.08; $c_L 2.56 \cdot .$ $.10^{-5}$ M, $c_S 4 \cdot .10^{-4}$ M, pH 5.21; $c_L 6.08 \cdot 10^{-5}$ M, $c_S 4 \cdot .10^{-4}$ M, pH 5.30).

$$\beta'_{2,4} = [VL_2S_4][V]^{-1}[L']^{-2}[S]^{-4}$$
(9)

[L'] is the dye conditional concentration in the presence of the surfactant ([HL] + [L]). Within the pH interval employed, the presence of both acid-base forms

of the dye and simultaneous absorbance by its ionized form must be assumed ((10)(11))

$$A = \varepsilon [VL_2S_4] + \varepsilon_L[L']$$
(10)
$$[VL_2S_4] = Y/Y_{max} c_L/2 ,$$

where $Y = \varepsilon [VL_2S_4] + \varepsilon_L[L'] - \varepsilon_Lc_L$,

$$Y_{\max} = \varepsilon c_{\rm L}/2 - \varepsilon_{\rm L} c_{\rm L} . \qquad (11)$$

The constant and molar absorption coefficient values are given in Table III. The presence of the VO_2^+ form can be assumed in solution at pH 2–3. At higher pH values cation hydrolysis and the polymerization equilibria can play a role, which is manifested as a decrease in the stability of the ternary complex.

Determination of vanadium. The stability of the ternary complex permits direct photometric determination of vanadium in a weakly acidic medium in the presence of small excesses of the dye and the surfactant. The colouration is developed instantaneously after mixing the components and remains constant for more than 24 hours in equimolar solutions. The absorbance of the dye – surfactant mixture slowly increases with time; this effects samples with low vanadium contents, e.g. the absorbance increases by 1-2% over 2 hours at $c_{\rm L} = 10c_{\rm V}$. For this reason it is recommended to always measure the solution absorbance at the same time after mixing the components, using water as a reference. At pH 4-5, 9-90 µg V can be reliably determined in 50 ml. The molar absorption coefficient, ε , equals 22:2. 10^3

$\log *\beta_{2,4}$	Ι	pН	$\varepsilon . 10^{-3} (nm)$	
 $18.25 + 0.1^{a}$	0.01	(2-3)	15·5 (670) ^d	
15·7 ^b	0.1	4.08	$22 \cdot 2 (630)^d$	
$14 \cdot 3^b$	0-1	5.21	$22 \cdot 1 (630)^e$	
14·7 ^b	0.01	5.30	_	
$14.6^{b,c}$	0.01	4.08		

TABLE III Equilibrium Constants of the Vanadium/Dye/Detergent Complex

^a Calculated from the pH-curve for equimolar solutions. ^b * $\beta_{2,4}$ recalculated from the conditional constants using the value, pK'_a 6-09. ^c Calculated from the Job curve for equimolar solutions $(c_0 \ 8. \ 10^{-5} \text{M}, c_{\rm S} > \text{cmc } 1.6. \ 10^{-3} \text{M})$. ^d $c_{\rm S} \ 1.2. \ 10^{-3} \text{M}$.

for a wavelength of λ 630 nm. The sensitivity on the Sandell scale is 0.0026 µg/cm² for ΔA 0.001. The coefficient of variation is 0.53% for 6 parallel determinations (1.06 µg V/ml; 95% probability level). The Fe³⁺, Fe²⁺, MoO₄²⁻, Th⁴⁺, ZrO²⁺, WO₄²⁻, Sb³⁺, UO₂²⁺, Ti⁴⁺, Pd²⁺, Sn⁴⁺ and CrO₄²⁻ ions interfere in the determination. Equimolar concentrations of Hg²⁺, Hg₂²⁺, PtCl₆²⁻, Co²⁺, Cu²⁺, Cd²⁺, Zn²⁺, Mn²⁺, Bi³⁺ and Au³⁺ ions do not interfere. The presence of the surfactant improves the selectivity of the determination. For example, Cu²⁺ ions react with the dye in pure solutions within the recommended pH interval, but their reaction is suppressed in the presence of a 10fold excess of Pb²⁺, a 20fold excess of La³⁺ and a 50fold excess of Ca²⁺, Ba²⁺, Mg²⁺, Al³⁺, Cr³⁺ or Ag⁺. The stability of the dye/surfactant binary complex decreases with increasing ionic strength and large concentrations of electrolytes and buffers may decrease the sensitivity of the determination (Tables II, III). This interference appears only at high concentrations; for example, a 2400fold excess of KCl (0.05m) causes a c. 10% decrease in the absorbance.

Procedure. To a 50 ml volumetric flask $10 \text{ ml } 10^{-3} \text{ m}$ dye solution are added 2.5 ml acetate buffer (pH 4), 15 ml 4. 10^{-3} m-CTA^+ solution and the sample containing 9–90 µg V. The mixture is diluted with water to the mark and the absorbance is measured after 10 minutes at 630 nm against water.

The authors are grateful to Mr J. Juřina, Department of Analytical and Organic Chemistry, for providing a sufficient amount of the dye and Mrs M. Kudlová for technical assistance.

REFERENCES

- 1. Bailey B. W., Chester J. E., Dagnall R. M., West I. S.: Talanta 15, 1359 (1968).
- Fendler E., Fendler J.: Advances in Physical Organic Chemistry, Vol. 8, p. 271. Academic Press, London-New York 1970.
- 3. Jencks W. P .: Kataliz v Khimii i Enzimologii. Mir, Moscow 1972.
- 4. Bruice T. C., Katzhendler J., Fedor L. R.: J. Amer. Chem. Soc. 90, 1333 (1968).
- 5. Svoboda V., Chromý V.: Talanta 13, 237 (1966).
- 6. Knowles J. R., Parson C. A.: Chem. Commun. 1967, 755.
- 7. Juřina J., Ružička E.: Unpublished results.
- 8. Cross J. T.: Analyst 90, 315 (1965).
- Uno T., Miyajima K., Tsukatani H.: Yakugaku Zasshi 80, 153 (1960); Chem. Abstr. 54, 11824e (1960).
- 10. Yoe J. A., Jones A. L.: Ind. Eng. Chem., Anal. Ed. 16, 11 (1944).
- 11. Job P.: Ann. Chim. (Paris) 9, 113 (1928).
- 12. Harvey A. E., Manning D. L.: J. Amer. Chem. Soc. 72, 4488 (1950).
- Sommer L., Kučerová J., Procházková H., Hniličková M.: Publ. Fac. Sci. Univ. Brno 1965, No 464, 249.
- Shinoda K., Nakagawa T., Tamamushi B., Isemura T.: Koloidnoe Poverkhnostnoaktivnye Veshchestva, p. 19. Mir, Moscow 1966.

Translated by M. Štulíková.